## SEA MATHS 2009

## Section 1



| No. | TEST ITEMS | WORKING COLUMN |  |  |  | Do Not Write Here |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  | KC | AT | PS |
| 5. | Carla scored 60 marks out of 75 on a Mathematics test. <br> Express Carla's score as a percentage. <br> Answer: 80\% | Maximum marks possible on the test $=75$ The score made by Carla $=60$. <br> Carla's score as a percent of the total: $\begin{gathered} =\frac{\text { Marks scored }}{\text { Maximum mark }} \times 100 \\ =\frac{60}{75} \times 100 \\ =80 \% \end{gathered}$ |  |  |  |  |  |  |
| 6. | Circle the LARGEST decimal fraction in the set below. <br> 0.43 <br> 0.6 <br> 0.079 <br> Answer: $0.43 \bigcirc 0.6079$ | We en place <br> The pl Tenths 0.43 h <br> 0.6 h <br> 0.079 <br> Theref | the de ue char <br> Tenths 0.1 <br> value Hundre 4 tenth 6 tenth 0 tent e, 0.6 i | imal fractio as follows <br> in order of ths, Thous <br> S <br> the largest. | s in a decimal <br> ize is; dths. |  |  |  |
| 7. | Each number in the pattern below is formed by removing 1 digit from the number above it. <br> Fill in the box to complete the pattern. <br> Answer: |  | The te the nu The te the nu <br> e, the e obta m the $n$ | s digit is re ber directly s digit is re ber directly ext numbe ed by rem mber direc | oved from above oved from above <br> in the pattern ving the 'tens y above, to get |  |  |  |


| No. | TEST ITEMS | WORKING COLUMN | Do Not Write Here |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | KC | AT | PS |
| 8. | What FRACTION of the entire shape below is shaded? <br> Answer: $\frac{5}{18}$ | The entire shape is composed of shaded and un-shaded equilateral triangles. <br> The total number of triangles, both shaded and un-shaded, in the shape is 18 The number of shaded triangles is 5 <br> The fraction of the shape that is shown shaded $\begin{aligned} & =\frac{\text { Number of shaded triangles }}{\text { Total number of triangles }} \\ & =\frac{5}{18} \end{aligned}$ |  |  |  |  |
| 9. | How many centimetres LONGER is John's pencil than Jeff's pencil? <br> Answer: $\mathbf{2 . 5} \mathbf{~ c m}$ | John's pencil measures 4.5 cm . Jeff's pencil measures 2 cm . John's pencil is $(4.5-2) \mathrm{cm}=2.5 \mathrm{~cm}$ longer than Jeff's pencil. |  |  |  |  |
| 10. | The length of the cuboid below is 10 cm . The area of the shaded face is $25 \mathrm{~cm}^{2}$. <br> Calculate the volume of the cuboid. <br> Answer: $\mathbf{2 5 0} \mathrm{cm}^{3}$ | Volume of the cuboid $\begin{aligned} & =\text { Area of shaded face } \times \text { Length } \\ & =(25 \times 10) \mathrm{cm}^{3} \\ & =250 \mathrm{~cm}^{3} \end{aligned}$ |  |  |  |  |


| No. | TEST ITEMS | WORKING COLUMN | Do Not Write Here |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | KC | AT | PS |
| 11. | The cost of a football and a cricket ball are shown below: <br> Football <br> Cricket ball <br> $\$ 199.00$ <br> $\$ 72.50$ <br> How much MORE does the football cost than the cricket ball? <br> Answer: \$126.50 | The football costs $\$ 199.00$ <br> The cricket ball costs $\$ 72.50$ <br> The football costs more that the cricket ball. <br> The football costs (\$199.00-\$72.50) more than the cricket ball. $\$ 199.00-$ <br> \$ 72.50 <br> $\$ 126.50$ <br> Hence, the football costs $\$ 126.50$ more <br> than the cricket ball. | Coser |  |  |
| 12. | Kyle started a test at 9:45 a.m. and finished at 11:30 a.m. How long did he take to complete the test? <br> Answer: 1 hour 45 minutes | Finish time on test $=11: 30 \mathrm{a} . \mathrm{m}$. <br> Start time $\quad=9: 45 \mathrm{a} . \mathrm{m}$. <br> Time taken to complete the test is found by subtraction. |  |  |  |
| 13. | The large cube below is built with small $1 \mathrm{~cm}^{3}$ blocks. <br> What is the volume of the cube? <br> Answer: 64 cm $^{3}$ | Each small cube has a volume of $1 \mathrm{~cm}^{3}$. <br> The large cube has 4 small cubes along its length, 4 along its width and 4 along its height. <br> Volume of the large cube $\begin{aligned} & =(4 \times 4 \times 4) \mathrm{cm}^{3} \\ & =64 \mathrm{~cm}^{3} \end{aligned}$ |  |  |  |


| No. | TEST ITEMS | WORKING COLUMN | Do Not Write Here |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | KC | AT | PS |
| 14. | A piece of paper in the shape of a circle has a diameter of 28 cm . The paper is folded equally 2 times to form the shape below. <br> What is the length of the side $\mathbf{a}$ ? <br> Answer: 14 cm | The original circle has a diameter of 28 cm as shown: <br> When folded once, the paper becomes semi-circular: <br> When folded a second time, the paper becomes a quarter circle, with radius, a, <br> a <br> The radius of a circle is one half of the diameter <br> The diameter of the circle $=28 \mathrm{~cm}$ The radius of the circle $=28 \div 2=14$ Length of $\mathbf{a}=14 \mathrm{~cm}$ |  |  |  |
| 15. | The scale below is balanced. EACH orange weighs 120 g . <br> What is the weight of the pineapple? <br> Answer: 840 g | The scale is balanced with 9 oranges on one side and 2 oranges and 1 pineapple on the other side. <br> If we remove 2 oranges from both sides of the scale, it will still be balanced. <br> Therefore, 7 oranges are equal in weight to 1 pineapple. <br> So, 1 pineapple weighs the same as the total weight of 7 oranges. $\begin{aligned} & =7 \times 120 \mathrm{~g} \\ & =840 \mathrm{~g} \end{aligned}$ |  |  |  |





## Section II

| No. | TEST ITEMS | WORKING COLUMN | Do Not Write Here |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | KC | AT | PS |
| 21. | Mr. Chin's supermarket has 15 rows of canned peas. Each row has 25 cans. <br> Calculate the TOTAL number of cans of peas in the supermarket. <br> Answer: 375 cans | $\begin{aligned} & \text { Number of rows of peas }=15 \\ & \text { Number of cans per row }=25 \\ & \text { Total number of cans } \\ & =\text { Number of rows } \times \text { Number of cans per row } \\ & =15 \times 25 \\ & =375 \end{aligned}$ |  |  |  |
| 22. | Four fractions are given below. $\frac{1}{3}, \quad \frac{1}{4}, \quad \frac{5}{6}, \quad \frac{5}{12}$ <br> Which THREE of these fractions when added result in a whole number? <br> Answer: $\frac{1}{3}, \frac{1}{4}$ and $\frac{5}{12}$ | The four given fractions are: $\frac{1}{3}, \frac{1}{4}, \frac{5}{6} \text { and } \frac{5}{12} .$ <br> Let us consider the denominators of each fraction, these are 3, 4, 6 and 12 . <br> A common denominator is 12 . If we express each fraction in twelfths it is easy to compare them. <br> We take $\frac{1}{3}$ and express it as $\frac{?}{12}$. Then repeat the process for the others. <br> $\times 4$ <br> Similarly, $\frac{1}{4}=\frac{3}{12}(\times 3) \quad \text { and } \quad \frac{5}{6}=\frac{10}{12}(\times 2)$ <br> So, the original fractions <br> 1155 <br> $\overline{3}, \frac{-}{4}, \overline{6}, \overline{12}$ <br> can be expressed as $\frac{4}{12}, \frac{3}{12}, \frac{10}{12}, \frac{5}{12}$ <br> To make up one whole we choose: $\frac{4}{12}+\frac{3}{12}+\frac{5}{12}=\frac{12}{12}=1$ |  |  |  |


| No. | TEST ITEMS | WORKING COLUMN | Do Not Write Here |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | KC | AT | PS |
| 23. | A class is building 6 model houses with lollipop sticks. Each house requires 879 lollipop sticks. Lollipop sticks are sold in packs of 100 . How many packs of sticks are needed to build these houses? <br> Answer: 53 packs | Number of sticks required per house $=879$ <br> Number of houses being built $=6$ <br> Number of sticks required $=879 \times 6=5274$ <br> The number of packs to be bought $=5274 \div 100$ <br> $=52$ and remainder 74 <br> Number of packs required is 52 full packs and 74 sticks from a $53^{\text {rd }}$ pack. <br> Number of packs of sticks required $=53$ |  |  |  |
| 24. | A class has 40 students. If 16 students are boys. What PERCENTAGE of the class are girls? <br> Answer: 60\% | Total number of students in class $=60$ <br> Number of boys $=16$ <br> The number of girls <br> $=$ Total number of students - Number of boys $\begin{aligned} & =40-16 \\ & =24 \end{aligned}$ <br> Percent of girls in the class: $\begin{aligned} & =\frac{\text { Number of girls }}{\text { Total number of students }} \times 100 \\ & =\frac{24}{40} \times 100 \\ & =60 \% \quad \text { OR } \end{aligned}$ <br> The percent of boys in the class $\begin{aligned} & =\frac{\text { Number of boys }}{\text { Total number of students }} \times 100 \\ & =\frac{16}{40} \times 100 \\ & =40 \% \end{aligned}$ <br> Hence the percentage that is girls $=(100-40)=60 \%$ |  |  |  |


| No. | TEST ITEMS | WORKING COLUMN | Do Not Write Here |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | KC | AT | PS |
| 25. | The diagram below shows two routes that Moe can walk to get from school to home. <br> How much longer is Route B than Route A? <br> Answer: $1 \frac{2}{15} \mathbf{k m}$ | From school to home by Route $\mathrm{A}=2 \frac{2}{3} \mathrm{~km}$ From school to home by Route $\mathrm{B}=3 \frac{4}{5}$ km . Route B is longer. <br> Route B is longer by $\left(3 \frac{4}{5}-2 \frac{2}{3}\right) \mathrm{km}$ $\begin{aligned} & =3 \frac{4}{5}-2 \frac{2}{3} \\ & =3 \frac{12}{15}-2 \frac{10}{15} \\ & =3-2+\frac{12}{15}-\frac{10}{15} \\ & =1 \frac{2}{15} \end{aligned}$ <br> Route B is $1 \frac{2}{15} \mathrm{~km}$ longer than Route A. |  |  |  |
| 26. | Mary has $\$ 40.00$. One half $\left(\frac{1}{2}\right)$ of Mary's money is equal to $\frac{2}{3}$ of Susie's money. <br> a) How much money does Susie have? <br> Answer: $\mathbf{\$ 3 0 . 0 0}$ <br> b) How much is $\frac{3}{8}$ of Mary's money? <br> Answer: \$15.00 | a) Mary has $\$ 40.00$ $\begin{aligned} & \frac{1}{2} \text { of Mary's money }=\frac{1}{2} \times \$ 40.00 \\ & =\$ 20.00 \end{aligned}$ $\begin{aligned} \text { Two thirds of Susie's money } & =\$ 20.00 \\ \text { One third of Susie's money } & =\$ 10 \\ \text { Three thirds of Susie's money } & =\$ 10 \times 3 \\ & =\$ 30 \end{aligned}$ $\text { b) } \begin{aligned} & \frac{3}{8} \text { of Mary, } \\ = & \frac{3}{8} \times \$ 40.00 \\ = & \frac{3}{8} \times \$ 40.00 \\ = & \$ 15.00 \end{aligned}$ |  |  |  |



| No. | TEST ITEMS | WORKING COLUMN | Do Not Write Here |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | KC | AT | PS |
| 28. | A library has 1200 books. Of these, $\frac{1}{4}$ are magazines and $\frac{2}{5}$ are story books. The remainder is textbooks. <br> a) How many magazines are there in the library? <br> Answer: $\mathbf{3 0 0}$ magazines <br> b) How many text books are there in the library? <br> Answer: 420 text books | Number of books in the library $=1200$ $\frac{1}{4}$ of the books are magazines <br> a) Number of magazines <br> $=\frac{1}{4}$ of 1200 <br> $=\frac{1}{4} \times 1200$ <br> $=300$ magazines <br> b) $\frac{2}{5}$ of the books are story books Number of story books $=\frac{2}{5} \times 1200$ $=480$ story books <br> Number of magazines + Number of story books $=300+480=780$ <br> Number of text books <br> $=1200-780$ <br> $=420$ text books <br> OR <br> Total fraction that comprises magazines and story books only $\begin{aligned} & =\frac{1}{4}+\frac{2}{5} \\ & =\frac{5}{20}+\frac{8}{20}=\frac{13}{20} \end{aligned}$ <br> Fraction that comprises text books $=1-\frac{13}{20}=\frac{7}{20}$ <br> Number of text books $\begin{aligned} & =\frac{7}{20} \times 1200 \\ & =420 \text { text books } \end{aligned}$ | $\sqrt{ }$ |  |  |




| No. | TEST ITEMS | WORKING COLUMN | Do Not Write Here |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | KC | AT | PS |
| 33. | A square and a rectangle are shown below. The perimeter of the square is twice the perimeter of the rectangle. <br> a) Calculate the perimeter of the square. <br> Answer: 48 cm <br> b) Calculate the length of ONE side of the square. <br> Answer: 12 cm | a) Perimeter of a rectangle $\begin{aligned} & =2(\text { Length }+ \text { Width }) \\ & =2(8+4) \mathrm{cm} \\ & =24 \mathrm{~cm} \end{aligned}$ <br> Perimeter of the square $\begin{aligned} & =2 \times \text { Perimeter of rectangle } \\ & =2 \times 24 \mathrm{~cm} \\ & =48 \mathrm{~cm} \end{aligned}$ <br> b) Perimeter of a square <br> $=4 \times$ length of side <br> Perimeter of the square $=48 \mathrm{~cm}$ <br> Length of side of square $=\frac{48 \mathrm{~cm}}{4}$ $=12 \mathrm{~cm}$ |  |  |  |
| 34. | The total mass of mangoes and oranges in a bag is 2 kg . Each orange has a mass of 50 g and each mango has a mass of 200 g . the bag contains 6 mangoes. <br> a) Calculate the TOTAL mass of the mangoes. <br> Answer: 1200 g <br> b) Calculate the number of oranges in the bag. <br> Answer: 16 oranges | a) Total mass of 6 mangoes, each of mass 200 g $\begin{aligned} & =200 \times 6 \mathrm{~g} \\ & =1200 \mathrm{~g} \end{aligned}$ <br> b) Total mass of mangoes and oranges $\begin{aligned} & =2 \mathrm{~kg} \\ & =2 \times 1000 \mathrm{~g} \quad[1 \mathrm{~kg}=1000 \mathrm{~g}] \\ & =2000 \mathrm{~g} \end{aligned}$ <br> The mass of oranges $\begin{aligned} & =\text { Total mass }- \text { mass of mangoes } \\ & =2000-1200 \mathrm{~g} \\ & =800 \mathrm{~g} \end{aligned}$ <br> Each orange has a mass of 50 g . <br> Number of oranges $\begin{aligned} & =\frac{\text { Total mass of oranges }}{\text { Mass of } 1 \text { orange }} \\ & =\frac{800 \mathrm{~g}}{50 \mathrm{~g}} \\ & =16 \text { oranges } \end{aligned}$ |  |  |  |



| No. | TEST ITEMS | WORKING COLUMN | Do Not Write Here |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | KC | AT | PS |
| 36. | The grid below is made up of 1 cm squares. Draw an isosceles triangle with a HEIGHT of 4 cm on the grid. <br> Answer: <br> [Other solutions are shown in the working column] | The diagrams below each show an isosceles triangle of height 4 cm . The length of the base varies. |  |  |  |






## Section III

| No. | TEST ITEMS | WORKING COLUMN | Do Not Write Here |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | KC | AT | PS |
| 41. | a) Street lights along a straight road are 20 m apart. What is the distance between the first street light and the tenth street light? <br> Answer: 180 m <br> b) A gardener decides to plant palm trees 10 m apart around a rectangular park. The park is 100 m long and 60 m wide. The diagram below shows where he digs the first and last holes for the first and last palm trees. <br> How many palm trees does he plant ALTOGETHER? <br> Answer: 27 trees | a) <br> Each street light is 20 m apart. <br> There are 9 equal distances of 20 m between the first and last street lights. Distance from the $1^{\text {st }}$ to the $10^{\text {th }}$ light: $\begin{aligned} & =20 \mathrm{~m} \times 9 \\ & =180 \mathrm{~m} \end{aligned}$ <br> b) <br> Observe that the number of equal distances between the first and last trees will always be one less than the number of trees. <br> Total distance from A to D $\begin{aligned} & =100+60+100 \\ & =260 \mathrm{~m} \end{aligned}$ <br> Plants 10 m apart <br> The number of equal intervals of 10 m between the first and last trees is: $=\frac{260}{10}=26$ <br> The number of trees is one more than the intervals $\begin{aligned} & =26+1 \\ & =27 \text { trees } \end{aligned}$ <br> [Note: if the counting were done in three stages, from $A$ to $B$, then $B$ to $C$ and then $C$ to $D$, care should be taken so that trees at points $B$ and $C$ are not counted twice.] |  |  |  |


| No. | TEST ITEMS |
| :---: | :---: |
| 42. | The diagram below shows the <br> number of points awarded for <br> striking the colours on a <br> dartboard. |

a) Tommy threw darts and struck green twice and red once. What was his TOTAL score?

## Answer: 70 points

b) Harry scored 100 points by striking each colour at least once. Complete the score sheet below to show how he scored the 100 points.

| Colour | No. of <br> times | Score |
| :--- | :---: | :---: |
| Blue |  |  |
| Green |  |  |
| Red | 2 | 60 |
| Total |  | 100 |

## Answer:

| Colour | No. of <br> times | Score |
| :--- | :---: | :---: |
| Blue | 2 | 20 |
| Green | 1 | 20 |
| Red | 2 | 60 |
| Total | 100 |  |

a) 2 green strikes at 20 points each, scores $20 \times 2=40$ points 1 red strike at 30 points $=30$ points
Total points scored by Tommy

$$
\begin{gathered}
=40+30 \\
=70 \text { points }
\end{gathered}
$$

b) Harry scores 100 points and strikes each colour at least once. He also scored 60 of these points by striking red twice.
Remaining points $=100-60=40$
He scored 40 points with at least one blue and one green:
1 blue +1 green
$=10+20$
$=30$ points
To score 40 points he needs to get 10 get more points, so he must strike another blue.

2 blue +1 green

$$
=2(20)+20
$$

$=40$ points
The table is complete with
2 blue strikes $=10 \times 2=20$ points
1 green strike $=20 \times 1=20$ points.
2 red strikes $=30 \times 2=60$ points
Total points obtained $=100$



| No. | TEST ITEMS | WORKING COLUMN | Do Not Write Here |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | KC | AT | PS |
| 45. | The diagram below shows a triangular prism. <br> a) How many faces of the prism are: <br> i. Triangular? <br> Answer: 2 faces <br> ii. Rectangular? <br> Answer: 3 faces <br> b) How many edges have a length of 45 cm ? <br> Answer: 3 edges <br> c) The volume of the prism is $90 \mathrm{~cm}^{3}$. It is cut into identical prisms each of volume $10 \mathrm{~cm}^{3}$. <br> What is the length of EACH of the smaller prisms? <br> Answer: 5 cm | a) (i) 2 triangular faces <br> Triangular faces <br> (ii) 3 rectangular faces <br> Rectangular faces <br> b) 3 edges have a length of 45 cm . <br> Length of 45 cm <br> c) Volume of prism $=90 \mathrm{~cm}^{3}$ <br> Each cut prism has a volume of 10 $\mathrm{cm}^{3}$ $\begin{aligned} & \text { Number of prisms cut }=\frac{90 \mathrm{~cm}^{3}}{10 \mathrm{~cm}^{3}} \\ & =9 \end{aligned}$ <br> Total length of all 9 prisms $=$ Length of the original uncut prism $=45 \mathrm{~cm}$ <br> Length of each of the prisms cut $\begin{aligned} & =\frac{45 \mathrm{~cm}}{9} \\ & =5 \mathrm{~cm} \end{aligned}$ | N |  |  |



