

JANUARY 2007 MATHEMATICS GENERAL PROFICIENCY (PAPER 2)

Section I

1. a. (i) **Required To Calculate:** 5.24(4-1.67) **Calculation:** 5.24(4-1.67) = 5.24(2.33) = 12.2092 (exactly) = 12.2 to 1 decimal place

- (ii) **Required To Calculate:** $\frac{1.68}{1.5^2 1.45}$
 - Calculation: $\frac{1.68}{1.5^2 - 1.45} = \frac{1.68}{2.25 - 1.45}$ $= \frac{1.68}{0.8}$ = 2.1 (exactly)
- b. Data: Aaron received 2 shares totaling \$60 from a sum shared in the ratio 2:5. Required To Calculate: The sum of money. Calculation:

Aaron's 2 shares total \$60 $\therefore 1 \text{ share } \equiv \frac{\$60}{2}$

= \$30

Total no. of shares = 2 + 5 = 7Sum that was shared altogether $= \$20 \times 7$

C.

$$= $30 \times 7$$

= \$210

Data: Cost of gasoline is \$10.40 for 3 litres. All currency in \$EC.

(i) **Required To Calculate:** Cost of 5 litres of gasoline. **Calculation:**

> If 3 litres of gasoline cost \$10.40 Then 1 litre of gasoline costs $\frac{\$10.40}{3}$ And 5 litres of gasoline cost $\frac{\$10.40}{3} \times 5$ = \$17.33<u>3</u> = \$17.33 to nearest cent



(ii) **Required To Calculate:** Volume of gasoline that can be bought with \$50.00.

Calculation:

\$10.40 affords 3 litres \$1.00 will afford $\frac{3}{10.40}$ litres \$50.00 will afford $\left(\frac{3}{10.40} \times 50.00\right)$ litres = 14.4 litres = 14 litres to the nearest whole number

2. a. **Data:** a = 2, b = -3 and c = 4

- (i) Required To Calculate: ab bcCalculation: ab - bc = 2(-3) - (-3)4= -6 + 12= 6
- (ii) Required To Calculate: $b(a-c)^2$ Calculation: $b(a-c)^2 = -3(2-4)^2$ $= -3(-2)^2$ = -3(4)

= -12

(i) **Data:** $\frac{x}{2} + \frac{x}{3} = 5$ **Required To Find:** x where $x \in Z$ **Solution:** $\frac{x}{2} + \frac{x}{3} = \frac{5}{1}$ $\times 6$ (x) = (x) = (5)

$$6\left(\frac{x}{2}\right) + 6\left(\frac{x}{3}\right) = 6\left(\frac{5}{1}\right)$$
$$3x + 2x = 30$$
$$5x = 30$$
$$x = 6 \in \mathbb{Z}$$

OR



$$\frac{x}{2} + \frac{x}{3} = 5$$
$$\frac{3(x) + 2(x)}{6} = 5$$
$$\frac{5x}{6} = 5$$
$$\times 6$$
$$5x = 30$$
$$x = 6 \in \mathbb{Z}$$

(ii) **Data:** $4 - x \le 13$ **Required To Find:** x where $x \in Z$ **Solution:** $4 - x \le 13$ $-x \le 13 - 4$

$$x \ge -9$$

 $\times -1$

That is $x = \{-9, -8, -7, ..., x \in Z\}$

c. **Data:** 1 muffin costs \$*m* and 3 cupcakes cost \$2*m*

(i) (a) **Required To Find:** Cost of five muffins in terms of m. **Solution:** 1 muffin costs m5 muffins costs $(m \times 5)$ = \$5m

(b) **Required To Find:** Cost of six cupcakes in terms of *m*. **Solution:**

If 3 cupcakes cost \$2*m*

Then 1 cupcake costs $\$\frac{2m}{3}$ And 6 cupcakes cost $\$\frac{2m}{3} \times 6$ = \$4m

(ii) **Required To Find:** An equation for the total cost of 5 muffins and 6 cupcakes is \$31.50.

Solution: 5m + 4m = 9mHence, 9m = 31.509m = 31.50



3. a. (i) **Data:**



Required To Describe: The shaded region using set notation. **Solution:**

The region shaded is all of sets A and B, that is $A \cup B$.

(ii) Data:



Required To Describe: The shaded region using set notation. **Solution:**

The region shaded is the region in U except $A \cup B$, that is $(A \cup B)'$.

(iii) Data:



Required To Describe: The shaded region using set notation. **Solution:**

The region shaded in the set A only. Hence the shaded region is A.

Data: $U = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}$

 $P = \{ \text{Prime numbers} \}$

 $Q = \{ \text{Odd numbers} \}$

Required To Draw: A Venn diagram to represent the information given. **Solution:**

 $P = \{2, 3, 5, 7\}$ $Q = \{1, 3, 5, 7, 9\}$

b.





c. **Data:** Venn diagram illustrating the number of elements in each region.



(i) **Required To Find:** No. of elements in $A \cup B$. Solution:



(ii) **Required To Find:** No. of elements in $A \cap B$. Solution:



 $n(A \cap B) = 4$

(iii)

Required To Find: No of elements in $(A \cap B)'$. **Solution:**

$$n(A \cap B)' = 10 + 3 + 8$$
$$= 21$$





(iv) **Required To Find:** No. of elements in U. **Solution:**



4. a. (i) **Required To Construct:** $\triangle ABC$ with BC = 6cm and AB = AC = 8cm. Solution:



(ii) **Required To Construct:** *AD* such that *AD* meets *BC* at *D* and is perpendicular to *BC*.



Solution:





b. **Data:**
$$P = (2, 4)$$
 and $Q = (6, 10)$



(i) **Required To Calculate:** Gradient of *PQ*. **Calculation:**

Gradient of
$$PQ = \frac{10-4}{6-2}$$
$$= \frac{6}{4}$$
$$= \frac{3}{2}$$

(ii) **Required To Calculate:** Midpoint of *PQ*. **Calculation:**

Let midpoint of PQ be M.

$$M = \left(\frac{2+6}{2}, \frac{4+10}{2}\right) = (4,7)$$

- 5. a. **Data:** $f(x) \rightarrow 7x + 4$ and $g(x) \rightarrow \frac{1}{2x}$
 - (i) Required To Calculate: g(3)Calculation:

$$g(3) = \frac{1}{2(3)}$$
$$= \frac{1}{6}$$

(ii) Required To Calculate: f(-2)Calculation: f(-2) = 7(-2) + 4= -14 + 4

$$= -10$$

5.0



(iii) Required To Calculate: $f^{-1}(11)$ Calculation: Let v = 7x + 4

Let
$$y = 7x + 4$$

 $y - 4 = 7x$
 $\frac{y - 4}{7} = x$
Replace y by x
 $\therefore f^{-1}(x) = \frac{x - 4}{7}$
 $\therefore f^{-1}(11) = \frac{11 - 4}{7}$
 $= \frac{7}{7}$
 $= 1$

b. (i) x = 5A'' = (1,2)

(ii)
$$B'' = (3,2)$$

C'' = (3, -1)

- (iii) Reflection in the line y = 4
- 6. **Data:** Table showing a frequency distribution of scores of 100 students in an examination.
 - (i) **Required To Complete:** And modify the table given. **Solution:**

Score (Discrete	U.C.B	Frequency	Cumulative	Points to Plot
Variable)			Frequency	(U.C.B, C.F.)
				(20, 0)
21 – 25	25	5	5	(25, 5)
26 - 30	30	18	18 + 5 = 23	(30, 23)
31 – 35	35	23	23 + 23 = 46	(35, 46)
36 - 40	40	22	22 + 46 = 68	(40, 68)
41 - 45	45	21	21 + 68 = 89	(45, 89)
46 - 50	50	11	11 + 89 = 100	(50, 100)
		$\sum c 100$		

$\sum f = 100$

The point (20, 0) corresponding to an upper class boundary of 20 and a cumulative frequency value of 0, obtained by checking 'backwards', is to be plotted, as the graph of cumulative frequency starts from the horizontal axis.

5.01'



(ii) Data: Scale is 2 cm to represent 5 units on the horizontal axis and 2 cm to represent 10 units on the vertical axis.
 Required To Plot: The cumulative frequency curve of the scores.
 Solution:

Cumulative Frequency Curve of Scores



(iii) **Required To Find:** Median score. Solution:

From the cumulative frequency curve, the median score corresponds to a cumulative frequency value of $\frac{1}{2}(100) = 50$ and reads as 36 on the horizontal axis. \therefore Median score = 36.



(iv) Required To Calculate: Probability a randomly chosen student has a score greater than 40.
 Solution:

 $P(\text{student chosen a trandom scores} > 40) = \frac{\text{No. of students scoring} > 40}{\text{Total no. of students}}$ $= \frac{21 + 11}{\sum f = 100}$ $= \frac{32}{100}$ $= \frac{8}{25}$

- 7. a. **Data:** Prism of cross-sectional area 144 cm^2 and length 30 cm.
 - (i) Required To Calculate: Volume of the prism. Calculation: Volume of prism = Area of cross-section × Length

$$=144\times30$$
 cm³

$$= 4320 \text{ cm}^3$$

(ii) **Required To Calculate:** Total surface area of the prism. **Calculation:**



Cross-section is a square of area 144 cm².

$$\therefore \text{Length} = \sqrt{144 \text{ cm}^2} = 12 \text{ cm}$$





Area of front and back faces $= 144 \times 2$ = 288 cm²

Area of L.H.S and R.H.S. rectangular faces = $2(12 \times 30)$ = 720 cm²

Area of top and base rectangular faces $= 2(12 \times 30)$ = 720 cm²

Total surface area of the prism = 288 + 720 + 720 $= 1728 \text{ cm}^2$

b. Data:



MON is a sector of a circle of radius 15 cm and $\hat{MON} = 45^{\circ}$.

(i) **Required To Calculate:** Length of minor arc *MN*. **Calculation:**

Length of arc
$$MN = \frac{45}{360} \times 2\pi(15)$$

= 11.775
= 11.78 cm to 2 decimal places

OR

Using $s = r\theta$ $s = \text{arc length}, r = \text{radius and } \theta = \text{angle in radians}$ s = (15)(0.785) = 11.775s = 11.78 cm to 2 decimal places



- (ii) Required To Calculate: Perimeter of figure MON. Calculation: Perimeter of MON = Arc length MON + Length of radius OM + Length of radius ON = 11.775 + 15 + 15 = 41.775 = 41.775 to 2 decimal places
- (iii) **Required To Calculate:** Area of figure *MON*. **Calculation:**

Area of sector $MON = \frac{45}{360} \times \pi (15)^2$ = 88.312 = 88.31cm² to 2 decimal places

OR

Area of sector
$$= \frac{1}{2}r^{2}\theta$$
$$= \frac{1}{2}(15)^{2}(0.785)$$
$$= 88.31\underline{2}$$
$$= 88.31 \text{ cm}^{2} \text{ to } 2 \text{ decimal places}$$

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8. **Data:** Table showing the subdivision of an equilateral triangle. **Required To Complete:** The table given.

n	Result of each step	No. of triangles formed
0		
		$1 = 4^{0}$
1		G
		$4 = 4^{1}$
2		
		$16 = 4^2$
3	605	(i) $64 = 4^3$
:		•
6		(ii) $4096 = 4^6$
:		:
(iii) 8		$65536 = 4^8$
		•
m		(iv) 4^m

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Section II

Required To Factorise: (i) $2p^2 - 7p + 3$, (ii) $5p + 5q + p^2 - q^2$ 9. a. **Factorising:**

(i)
$$2p^2 - 7p + 3$$

= $(2p-1)(p-3)$

(ii)
$$5p + 5q + p^2 - q^2$$

= $5(p+q) + (p-q)(p+q)$
= $(p+q)\{5 + (p-q)\}$
= $(p+q)(5 + p-q)$

Required To Expand: $(x+3)^2(x-4)$ b. Solution: Expanding $(x+3)^2(x-4) = (x+3)(x+3)(x-4)$

$$= (x^{2} + 3x + 3x + 9)(x - 4)$$

= $(x^{2} + 6x + 9)(x - 4)$
= $x^{3} + 6x^{2} + 9x - 4x^{2} - 24x - 36$
= $x^{3} + 2x^{2} - 15x - 36$

Hence, $(x+3)^2(x-4) = x^3 + 2x^2 - 15x - 36$, in descending powers of *x*.

c. **Data:**
$$f(x) = 2x^2 + 4x - 5$$

Required To Express: $f(x) = 2x^2 + 4x - 5$ in the form $a(x+b)^2 + c$. (i) Solution:

$$f(x) = 2x^2 + 4x - 5$$

= 2(x² + 2x) - 4

 $= 2(x^{2} + 2x) - 5$ (Half the coefficient of x is $\frac{1}{2}(2) = 1$) Hence $f(x) = 2x^{2} + 4x - 5$ $= 2(x + 1)^{2} + *$ $= 2(x^{2} + 2x + 1) + *$

-5

$$= 2x^{2} + 4x + 2$$
 (Hence * = -7)
-7

 $\therefore 2x^2 + 4x - 5 \equiv 2(x+1)^2 - 7$ is of the form $a(x+b)^2 + c$ where

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 $a = 2 \in \Re$ $b = 1 \in \Re$ $c = -7 \in \Re$

OR

$$2x^{2} + 4x - 5 = a(x + 5)^{2} + c$$

$$= a(x^{2} + 2bx + b^{2}) + c$$

$$= ax^{2} + 2abx + ab^{2} + c$$

Equating coefficient of x^{2} .

$$a = 2 \in \Re$$

Equating coefficient of x .

$$2(2)b = 4$$

$$b = 1 \in \Re$$

Equating constants.

$$2(1)^{2} + c = -5$$

$$c = -7 \in \Re$$

$$\therefore 2x^{2} + 4x - 5 \equiv 2(x + 1)^{2} - 7$$

(ii) **Required To Find:** The equation of the axis of symmetry. **Solution:**

If $y = ax^2 + bx + c$ is any quadratic curve, the axis of symmetry has equation $x = \frac{-b}{2a}$.

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The equation of the axis of symmetry in the quadratic curve

$$f(x) = 2x^{2} + 4x - 5$$
 is $x = \frac{-(4)}{2(2)}$
 $x = -1$

(iii) **Required To Find:** Coordinates of the minimum point on the curve. **Solution:**

$$f(x) = 2x^{2} + 4x - 5$$

= 2(x + 1)² - 7
2(x + 1)² \ge 0 \forall x
\therefore f(x)_{min} = -7 at 2(x + 1)^{2} = 0
x = -1



(iv) - (v)

Required To Draw: The graph of f(x) showing the minimum point and the axis of symmetry.

Solution:



- 10. Data: Pam must buy x pens and y pencils.
 - a. (i) **Data:** Pam must buy at least 3 pens. **Required To Find:** An inequality to represent the above information. **Solution:** No. of pens bought = xNo. of pens is at least 3. $\therefore x \ge 3$
 - (ii) Data: Total number of pens and pencils must not be more than 10.
 Required To Find: An inequality to represent the above information.
 Solution:

No. of pencils = y Total number of pens and pencils = x + y $\therefore (x + y)$ is not more than 10. $\therefore x + y$ is less than or equal to 10. $x + y \le 10$

(iii) **Data:** $5x + 2y \le 35$ **Required To Find:** Information represented by this inequality. **Solution:** $5x + 2y \le 35$ (data) 5x represents the cost of x pens at \$5.00 each and 2y represents the cost of y pencils at \$2.00 each. Total cost is 5x + 2y.



Since $5x + 2y \le 35$, then the total cost of *x* pens and *y* pencils is less than or equal to \$35.00 That is, the total cost of the *x* pens and *y* pencils is not more than \$35.00.



Solution:

The line x = 3 is a vertical line. The region $x \ge 3$ is



Obtaining 2 points on the line x + y = 10

When x = 0 0 + y = 10y = 10

The line x + y = 10 passes through the point (0, 10). When y = 0 x + 0 = 10

x = 10

The line x + y = 10 passes through the point (10, 0).



The region with the smaller angle satisfies the \leq region. The region with satisfies $x + y \leq 10$ is





The graph of the line 5x + 2y = 35 was given. It passes through the points (7, 0) and (3, 10).



The region with the smaller angle satisfies the \leq region. The region which satisfies $5x + 2y \leq 35$ is



The line y = 0 is the horizontal x – axis. The region which satisfies $y \ge 0$ is





The region which satisfies all four inequalities is the area in which all four previously shaded regions overlap. The region which satisfies all four inequalities is



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(ii) **Required To Find:** The vertices of the region bounded by the 4 inequalities is shown ABCD (the feasible region) **Solution:** A(3,0) B(3,7) C(5,5) D(7,0)



- c. **Data:** A profit of \$1.50 is made on each pen and a profit of \$1.00 is made on each pencil.
 - (i) **Required To Find:** The profit in terms of x and y. **Solution:**

Let the total profit on pens and pencils be *P*. The profit on *x* pens at $\$1\frac{1}{2}$

and y pencils at \$1 each =
$$\left(x \times 1\frac{1}{2}\right) + \left(y \times 1\right)$$

 $\therefore P = 1\frac{1}{2}x + y$

(ii) **Required To Find:** Maximum profit. **Solution:**

Choosing only *B* (3, 7), *C* (5, 5) and *D* (7, 0). At *B* x = 3 y = 7

$$P = 3\left(1\frac{1}{2}\right) + 7$$
$$= \$11\frac{1}{2}$$

$$2 = $11.50$$

A

t
$$C x = 5$$
 $y = 5$

$$P = 5\left(1\frac{1}{2}\right) + 5$$
$$= \$12\frac{1}{2}$$
$$-\$12.50$$

At
$$D \ x = 7$$
 $y = 0$
 $P = 7\left(1\frac{1}{2}\right)$
 $= \$10\frac{1}{2}$
 $= \$10.50$

: Maximum profit made is \$12.50 when Pam buys 5 pens and 5 pencils.



(iii) Required To Find: The maximum number of pencils Pam can buy if she buys 4 pens.



When x = 4 the maximum value of $y \in Z^+$ is 6. Therefore, when 4 pens are bought, the maximum number of pencils that can be bought that satisfies all conditions is 6.



11. a. **Data:** Diagram showing 2 circles of radii 5 cm and 2 cm touching at *T*, *XSRY* is a straight line touching the circles at *S* and *R*.



 $P\hat{S}R = Q\hat{R}S = 90^{\circ}$



(Angle made by a tangent to a circle and the radius, at the point of $contact = 90^{\circ}$).



There are corresponding angles, when *PS* is parallel to *QR* and *SR* is a transversal.

(ii) **Data**: N is a point such that QN is perpendicular to PS.





b. **Data:** Circle, centre *O* and $\hat{MOL} = 110^{\circ}$.



(i) **Required To Calculate:** *MNL* **Calculation:**

$$\hat{MNL} = \frac{1}{2} (110^{\circ})$$
$$= 55^{\circ}$$

(Angle subtended by a chord at the centre of a circle is twice the angle it subtends at the circumference, standing on the same arc).

(ii) Required To Calculate: $L\hat{M}O$ Calculation: OM = OL (radii) $L\hat{M}O = \frac{180^\circ - 110^\circ}{2}$

(Base angles of an isosceles triangle are equal and sum of the angles in a triangle = 180°).

- 12. Data: The distances and directions of a boat traveling from A to B and then to C.
 - a. **Required To Draw:** Diagram of the information given, showing the north direction, bearings 135° and 060° and distances 8 km and 15 km. Solution:





b. (i) **Required To Calculate:** The distance AC. **Calculation:** $A\hat{B}C = 45^\circ + 60^\circ$ $= 105^\circ$ $AC^2 = (15)^2 + (8)^2 - 2(15)(8)\cos 105^\circ (\cos ine \, law)$ $= 18.738 \, \text{km}$ $= 18.74 \, \text{km}$ to 2 decimal places

(ii) **Required To Calculate:** \hat{BCA} **Calculation:**

Let
$$B\hat{C}A = \theta$$

 $\frac{15}{\sin\theta} = \frac{18.738}{\sin 105^{\circ}} (\sin law)$
 $\therefore \sin\theta = \frac{15\sin 105^{\circ}}{18.738}$
 $= 0.7732$
 $\therefore \theta = \sin^{-1}(0.7732)$
 $\theta = 50.64^{\circ}$
 $= 50.6^{\circ}$ to the nearest 0.1°

(iii) **Required To Calculate:** The bearing from *A* from *C*. **Calculation:**



The bearing of A from $C = 180^\circ + 60^\circ + 50.64^\circ$ = 290.64°

 $= 290.6^{\circ}$ to the nearest 0.1°

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13. **Data:** Vector diagram with $\overrightarrow{OP} = \underline{r}$, $\overrightarrow{PM} = \underline{s}$ and OMN a straight line with midpoint *M*.

$$\overrightarrow{OX} = \frac{1}{3}\overrightarrow{OM}$$
 and $\overrightarrow{PX} = 4\overrightarrow{XQ}$

a. **Required To Sketch:** Diagram illustrating the information given. **Solution:**



- b. (i) **Required To Express:** \overrightarrow{OM} in terms of \underline{r} and \underline{s} . **Solution:** $\overrightarrow{OM} = \overrightarrow{OP} + \overrightarrow{PM}$ $= \underline{r} + \underline{s}$
 - (ii) **Required To Express:** \overrightarrow{PX} in terms of \underline{r} and \underline{s} . Solution:

$$\overrightarrow{OX} = \frac{1}{3} \overrightarrow{OM}$$
$$= \frac{1}{3} (\underline{r} + \underline{s})$$
$$\overrightarrow{PX} = \overrightarrow{PO} + \overrightarrow{OX}$$
$$= -(\underline{r}) + \frac{1}{3} (\underline{r} + \underline{s})$$
$$= -\frac{2}{3} \underline{r} + \frac{1}{3} \underline{s}$$

(iii) **Required To Express:** \overrightarrow{QM} in terms of \underline{r} and \underline{s} . Solution:

$$\overrightarrow{PX} = 4\overrightarrow{XQ}$$
$$\overrightarrow{PQ} = \frac{5}{4}\overrightarrow{PX}$$
$$= \frac{5}{4}\left(-\frac{2}{3}\overrightarrow{r} + \frac{1}{3}\overrightarrow{s}\right)$$



$$\overrightarrow{PQ} = -\frac{5}{6}\underline{r} + \frac{5}{12}\underline{s}$$
$$\overrightarrow{QM} = \overrightarrow{QP} + \overrightarrow{PM}$$
$$= -\left(-\frac{5}{6}\underline{r} + \frac{5}{12}\underline{s}\right) + \underline{s}$$
$$= \frac{5}{6}\underline{r} + \frac{7}{12}\underline{s}$$

Required To Prove: $\overrightarrow{PN} = 2\overrightarrow{PM} + \overrightarrow{OP}$ c. **Proof:**

Required to Prove:
$$PN = 2PM + OP$$

Proof:
 $2\overrightarrow{PM} = 2(\underline{s})$
 $\overrightarrow{OP} = \underline{r}$
 $2\overrightarrow{PM} + \overrightarrow{OP} = 2\underline{s} + \underline{r}$
 $= \underline{r} + 2\underline{s}$
Hence, $\overrightarrow{PN} = 2\overrightarrow{PM} + \overrightarrow{OP}$ $(= \underline{r} + 2\underline{s})$
Q.E.D

14. a. Data:
$$D = \begin{pmatrix} 1 & 9p \\ p & 4 \end{pmatrix}$$

Required To Calculate: p
Calculation:
If $D = \begin{pmatrix} 1 & 9p \\ p & 4 \end{pmatrix}$ is singular then det $D = 0$
 $\therefore (1 \times 4) - (9p \times p) = 0$
 $4 = 9p^2$
 $p^2 = \frac{4}{9}$
 $p = \sqrt{\frac{4}{9}}$
 $= \pm \frac{2}{3}$
Hence, $p = \pm \frac{2}{3}$.



- b. **Data:** 2x + 5y = 6 and 3x + 4y = 8
 - (i) **Required To Express:** The above equations in the form AX = B. Solution:

2x + 5y = 6 3x + 4y = 8Hence, $\begin{pmatrix} 2 & 5 \\ 3 & 4 \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} 6 \\ 8 \end{pmatrix}$...matrix equation is of the form AX = B where $A = \begin{pmatrix} 2 & 5 \\ 3 & 4 \end{pmatrix}$ $X = \begin{pmatrix} x \\ y \end{pmatrix}$ and $B = \begin{pmatrix} 6 \\ 8 \end{pmatrix}$ are matrices. (ii) (a) Required To Calculate: Determinant of A. Calculation: Det A = (2 × 4) - (5 × 3) = 8 - 15 = -7

(b) **Required To Prove:** $A^{-1} = \begin{pmatrix} -\frac{4}{7} & \frac{5}{7} \\ \frac{3}{7} & -\frac{2}{7} \end{pmatrix}$.

Proof:

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$$A^{-1} = -\frac{1}{7} \begin{pmatrix} 4 & -(5) \\ -(3) & 2 \end{pmatrix}$$
$$= \begin{pmatrix} -\frac{4}{7} & \frac{5}{7} \\ \frac{3}{7} & -\frac{2}{7} \end{pmatrix}$$
Q.E.D.



Required To Calculate: *x* and *y* (c) **Calculation:** AX = B $\times A^{-1}$ $A \times A^{-1} \times X = A^{-1} \times B$ $I \times X = A^{-1}B$ $X = A^{-1}B$ and $\begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} -\frac{4}{7} & \frac{5}{7} \\ \frac{3}{7} & -\frac{2}{7} \end{pmatrix} \begin{pmatrix} 6 \\ 8 \end{pmatrix}$ C $\begin{pmatrix} -\frac{4}{7} \times 6 \end{pmatrix} + \begin{pmatrix} \frac{5}{7} \times 8 \end{pmatrix}$ $\begin{pmatrix} \frac{3}{7} \times 6 \end{pmatrix} + \begin{pmatrix} -\frac{2}{7} \times 8 \end{pmatrix}$ = $-\frac{40}{7}$ $\frac{\frac{24}{7}}{\frac{18}{7}}$ $\frac{2}{7}$ $\frac{2}{7}$ $\frac{2}{7}$ Equating corresponding $x = 2\frac{2}{7}$ and $y = \frac{2}{7}$.

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